

Table 5. *Principal axes of thermal ellipsoids*

$\alpha, \beta, \gamma$  are the direction cosines relative to the crystallographic axes  $a, b, c$ .  $D$  is the mean square displacement of the atom in the given direction.

	$\alpha$	$\beta$	$\gamma$	$D$
S	0.3166 0.6991 0.6412	0.1076 0.6451 -0.7564	0.9426 -0.3081 -0.1286	0.0529 0.0411 0.0325
C(1)	0.8405 0.1195 0.5283	0.4295 -0.7413 -0.5156	-0.3300 -0.6603 0.6744	0.0726 0.0315 0.0189
C(2)	0.1277 0.9534 0.2732	-0.6699 0.2860 -0.6850	0.7313 0.0955 -0.6752	0.0207 0.0676 0.0505
N(1)	0.4605 0.7643 0.4511	0.2077 -0.5870 0.7824	-0.8629 0.2666 0.4292	0.1130 0.0583 0.0404
N(2)	0.4984 0.3990 0.7695	-0.8053 0.5416 0.2407	0.3207 0.7398 -0.5914	0.0378 0.1007 0.0818

The direction cosines of the principal axes of the thermal ellipsoids and the mean square amplitudes of vibration are given in Table 5. The anisotropies are not large, and there does not appear to be anything unusual about the vibrations of the molecule.

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to thank the Chemistry Department of that Institute for the award of an A.A. Noyes postdoctoral fellowship at that time. The computer center at Montana State University has made its facilities freely available for the computations required in this determination.

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## The Crystal Structure of ThTi<sub>2</sub>O<sub>6</sub> (Brannerite)

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ThTi<sub>2</sub>O<sub>6</sub>, synthesized at 1610°C by solid-state reaction, crystallizes in the monoclinic system, space group *C2/m*, with the unit-cell dimensions  $a=9.822$ ,  $b=3.824$ ,  $c=7.036$  Å,  $\beta=118.84^\circ$ . It contains layers formed by Ti-O octahedra sharing edges and corners in a manner reminiscent of the anatase structure, and these are joined through thorium ions in interlayer octahedral positions. There are two Th-O distances of 2.36 Å and four of 2.35 Å, but the octahedron is flattened; two more oxygen atoms further away at 2.96 Å are probably unbonded. Ti-O distances ranging from 1.83 to 2.20 Å are normal. The structure was determined by Fourier methods and refined by several three-dimensional least-squares cycles.

### Introduction

One of the gaps of appreciable magnitude in the structural inorganic chemistry of solids is listed in *Dana's System of Mineralogy* (1944, p.745 *et seq.*) under the

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general title 'multiple oxides containing columbium (sic), tantalum and titanium'. These minerals contain a wide variety of substituent elements which may include the actinide elements thorium and uranium, and many of them are found in the *metamict* state. Although seeming to form crystals with extensive facial development, metamict minerals are imperfectly crystallized or even glassy substances, and it is widely believed that

they have undergone extensive radiation damage during the course of time. This could have resulted either from the disintegration of radio-elements originally present in the structure, or from a nuclear bombardment originating at some nearby external natural source. Metamict crystals can be recrystallized by heating but become polycrystalline, and doubts are raised whether or not a reconstituted specimen is identical in structure with the primordial mineral. It is therefore difficult to select naturally occurring specimens belonging to this general class, and new synthetic materials must be provided for detailed study.

Patchett & Nuffield (1960) prepared  $\text{UTi}_2\text{O}_6$  and showed that its symmetry and unit-cell size were compatible with the morphological form development of metamict brannerite recorded by Pabst (1954), and also with powder diffraction patterns of the recrystallised mineral. The compound is not isomorphous with any other  $\text{AB}_2\text{O}_6$  compound, despite an earlier report that  $\text{UTi}_2\text{O}_6$  made at  $1000^\circ\text{C}$  had the columbite structure (Schröke, 1958).

Although thorium is recorded in most chemical analyses of brannerite as a minor replacement element, there is no known mineral analogue where it is an essential constituent (Fron del, 1956). Nevertheless  $\text{ThTi}_2\text{O}_6$  was shown to exist in high- and low-temperature varieties (Perez y Jorba, Mondange & Colongues, 1961), but neither set of lattice parameters determined from Guinier powder patterns bore any obvious resemblance to those of  $\text{UTi}_2\text{O}_6$  or columbite. We decided to examine  $\text{ThTi}_2\text{O}_6$ , and it has proved to be isostructural with  $\text{UTi}_2\text{O}_6$  with a new type of crystal structure, which can be regarded as a derivative of the anatase form of  $\text{TiO}_2$ .

### Experimental

$\text{ThTi}_2\text{O}_6$  was prepared by dry mixing weighed amounts of high purity  $\text{ThO}_2$  and  $\text{TiO}_2$ , pressing into wafers, and then firing to  $1610^\circ\text{C}$  for one hour in vacuum. One specimen, heated at  $1000^\circ\text{C}$  in air for a further period of twelve hours, turned from black to light buff without any obvious change of powder pattern. This provided the crystal for the present study. The symmetry and approximate unit-cell size were determined by single-crystal methods, and accurate values of  $\sin^2\theta$  for the low-angle reflexions were obtained on a Guinier-type focusing camera internally calibrated with potassium chloride (Table 1). The more precise lattice parameters listed in Table 2 were evaluated from these measurements by a least-squares fit. Table 2 also includes the data reported for  $\text{UTi}_2\text{O}_6$  by Patchett & Nuffield (1960). The two compounds are clearly isostructural, with Th and U playing the same role in both structures.

This unit-cell assignment does not agree with that reported by Perez y Jorba *et al.* (1961) for either form of  $\text{ThTi}_2\text{O}_6$ . Their low temperature variety was stated to be orthorhombic with the unit-cell dimensions  $a=16.7$ ,  $b=14.95$ ,  $c=4.1$  Å, while the high-temperature

Table 1. Powder pattern of  $\text{ThTi}_2\text{O}_6$ , Cu  $K\alpha_1$

<i>l</i> (obs.)	$\sin^2 \theta$ (obs.)	$\sin^2 \theta$ (calc.)	<i>hkl</i>
<i>mw</i>	0.01561	0.01563	001
<i>ms</i>	0.02607	0.02611	20 $\bar{1}$
<i>mw</i>	0.03206	0.03209	200
<i>ms</i>	0.04862	0.04861	110
<i>m</i>	0.05141	0.05141	20 $\bar{2}$
<i>w</i>	0.05339	0.05345	11 $\bar{1}$
<i>w</i>	0.06251	0.06253	002
<i>mw</i>	0.06934	0.06933	201
<i>w</i>	0.07507	0.07505	111
<i>mw</i>	0.08958	0.08955	11 $\bar{2}$
<i>mw</i>	0.09604	0.09604	31 $\bar{1}$
<i>vw</i>	0.10078	0.10077	40 $\bar{1}$
<i>vw</i>	0.11055	0.11054	31 $\bar{2}$
<i>w</i>	0.11280	0.11281	310

Table 2. Lattice parameters of  $\text{ThTi}_2\text{O}_6$  with those of  $\text{UTi}_2\text{O}_6$  (Patchett & Nuffield, 1960) included for comparison

	$\text{ThTi}_2\text{O}_6$	$\text{UTi}_2\text{O}_6$
<i>a</i>	$9.822 \pm 0.005$ Å	9.87 Å
<i>b</i>	$3.824 \pm 0.002$	3.76
<i>c</i>	$7.036 \pm 0.005$	6.95
$\beta$	$118.84 \pm 0.05^\circ$	$119.5^\circ$
Unit-cell volume	$231.4$ Å <sup>3</sup>	$224.5$ Å <sup>3</sup>
$D_m$	$6.0 \pm 0.5$ g.cm <sup>-3</sup>	6.36 g.cm <sup>-3</sup>
$D_x$	6.08 g.cm <sup>-3</sup>	6.35 g.cm <sup>-3</sup>
<i>Z</i>	2	2
Systematic absent reflexions	<i>hkl</i> with $h+k \neq 2n$	
Space group alternatives	<i>C</i> 2,	<i>C</i> m, <i>C</i> 2/ <i>m</i>

form was considered tetragonal with  $a=7.58$ ,  $c=10.45$  Å. Indeed the powder data in Table 1 can be indexed very roughly on this latter basis which, in view of the present new evidence, must be considered incorrect.

Intensity data were collected from a colourless crystal  $0.15 \times 0.05 \times 0.05$  mm oriented for rotation about the *b* axis. The levels *hkl*, with  $k=0, 1 \dots 5$  were recorded by the integrating Weissenberg method, using filtered molybdenum radiation to reduce absorption. Three films interleaved with tinfoil were used for each level. Intensities were measured by visual comparison with a calibrated film strip, and specimen absorption was neglected for such a small crystal. Scattering curves for  $\text{Th}^{4+}$  and  $\text{Ti}^{4+}$  were from the compilation of Cromer & Waber (1965) based upon relativistic Dirac-Slater wave functions, and corrected for both real and imaginary components of the anomalous scattering for Mo  $K\alpha$ , while Suzuki's data for  $\text{O}^{2-}$  were used for oxygen.

A total of 296 non-symmetry-related reflexions were recorded, and these data, scaled by comparison with structure factors calculated for the final model, are given in Table 3. All calculations were made on the Division's Elliott 803 Computer with the programming system of Daly, Stephens & Wheatley (1963) kindly made available by Dr P.J. Wheatley.

Structure determination

A satisfactory solution of the structure was found by assuming the space group C2/m, and no attempt was made to lower the symmetry group to either of the two possible alternatives, C2 or Cm. As there are two formula units in the unit cell, the Th atom can be placed at the origin in the point position 2(a). A projection of the Patterson function P(u,w) immediately gave an approximate position for Ti in a general position 4(i). Fourier projections on to (010) were made, one a normal F<sub>o</sub> synthesis and the other with the Th atom excluded in a partial difference map. Two of the three oxygen atoms were clearly visible in this latter case (Fig. 1), while the contours of the Ti atom were rather elongated, suggesting that the third oxygen atom was overlying it in the projection.

From this it was possible to derive a complete structure satisfying the space group and formula criteria. Refinement continued with a number of three-dimensional least-squares cycles, using individual isotropic temperature factors for each atom. The weighting scheme of Cruickshank (1961):

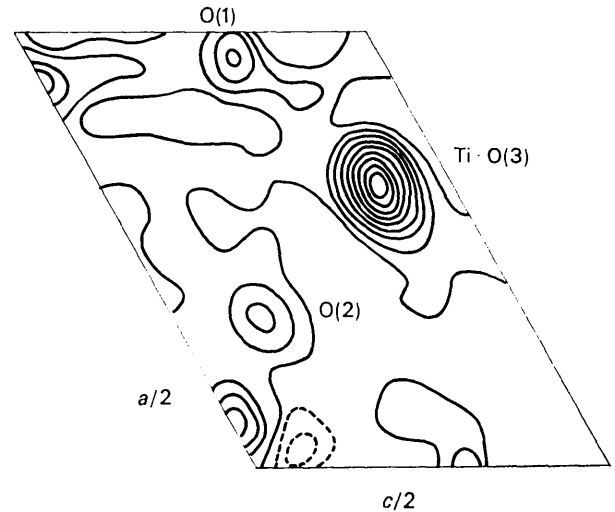


Fig. 1. F<sub>o</sub> - F<sub>Th</sub> projection on to (010), contoured at arbitrary intervals. Ti (plus an overlying oxygen atom), and two additional oxygen atoms are visible. There is evidence at (0,0) for anisotropic thermal motion of the Th, removed from this position.

Table 3. Observed and calculated structure factors (x 10)

Table with 16 columns: h, k, l, F<sub>o</sub>, F<sub>c</sub> repeated four times. It contains numerical data for various Miller indices (hkl) and their corresponding observed (F<sub>o</sub>) and calculated (F<sub>c</sub>) structure factors.

Table 4. Fractional atomic coordinates and standard deviations

Table with 6 columns: Point position, x, y, z, sigma(x), sigma(z), B (A^2), sigma(B). It lists the fractional coordinates and standard deviations for Th(1), Ti(1), O(1), O(2), and O(3) in the space group C2/m.

$$w = \frac{1}{a + |F_o| + c|F_o|^2}, \quad a = 2|F_{\min}|, \quad c = \frac{2}{|F_{\max}|}$$

was adopted, and the matrix inversion involved the block diagonal approximation.

After each cycle the scaling factors for the various levels were adjusted by comparison with the calculated structure amplitudes. It soon became obvious that the  $h3l$  data were not as accurate as those from other levels owing to some malfunction of the camera during the lengthy exposure. Consequently the reflexions from this level were excluded, and the refinement continued until shifts of thermal and positional parameters were less than one-fourth the estimated standard deviations. These parameters are listed in Table 4. Finally three further cycles were made assuming the Th and Ti atoms were vibrating anisotropically. There is some evidence for this in the partial difference map (Fig. 1). This reduced the  $R$  value for the five levels of data from 14.3 to 11.6%. The corrections to the metal atoms expressed as the six mean-square-amplitude tensors  $U_{ij}$  (Cruickshank, 1965) are given in Table 5, and were used in

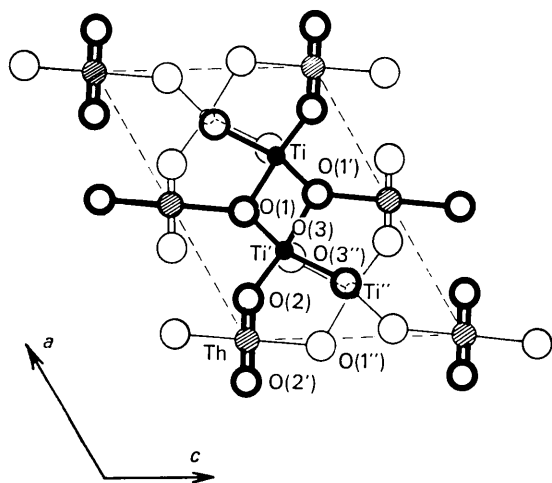


Fig. 2. Structure of  $\text{ThTi}_2\text{O}_6$ . Smallest circles Ti, largest O. The Th atoms are hatched.

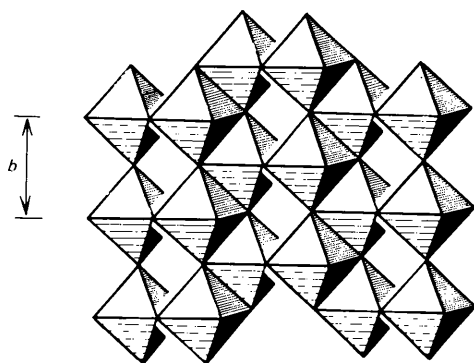


Fig. 3. A sheet of Ti-O octahedra, forming the basis of the structure of  $\text{ThTi}_2\text{O}_6$ .

the final calculations of structure factors (Table 3). The  $h3l$  terms are also included in this table; their inclusion raised the overall  $R$  value from 11.6 to 12.2%.

Table 5. Anisotropic thermal corrections to metal atoms

	Mean-square-amplitude tensors $U_{ij}$					
	$U_{11}$	$U_{22}$	$U_{33}$	$2U_{12}$	$2U_{23}$	$2U_{13}$
Th(1)	0.0271	0.0152	0.0115	0.0000	0.0000	0.0100
Ti(1)	0.0318	0.0180	0.0180	0.0000	0.0000	0.0066

### Description

The structure is illustrated as a ball-and-spoke drawing in Fig. 2 and as an assemblage of octahedra in Fig. 4(a). All the atoms are located in mirror planes normal to the  $b$  axis and at the two levels,  $y=0$  and  $\frac{1}{2}$ . There are two Ti atoms at  $y=\frac{1}{2}$  octahedrally coordinated to oxygen and joined by a common edge [the atoms O(1)], while identical pairs centred at  $y=0$  are united to it at opposite ends by additional edge-sharing. These build up into infinite zigzag sheets centred about the (100) planes (Fig. 3) and there are no atoms common to adjacent sheets. These Ti-O octahedra, all of which are crystallographically identical, are somewhat distorted (Table 6), the Ti-O distances ranging from  $1.83 \pm 0.04 \text{ \AA}$  to  $2.20 \pm 0.07 \text{ \AA}$  with an average value of  $1.97 \text{ \AA}$ . The shortest oxygen-oxygen distance of  $2.41 \pm 0.06 \text{ \AA}$  is between the atoms O(1).

Table 6. Interatomic distances and *e.s.d*'s ( $\text{\AA}$ )

Th—O(2)	$2.35 \pm 0.04$ (4)
Th—O(1'')	$2.36 \pm 0.05$ (2)
O(2)—O(2')	$2.76 \pm 0.06$ (2)
O(2)—O(1'')	$3.38 \pm 0.06$ (8)
O(2)—O(2)	3.824 (2)
Ti—O(1)	$1.83 \pm 0.04$ (1)
Ti—O(2)	$1.83 \pm 0.05$ (1)
Ti—O(3)	$1.94 \pm 0.07$ (2)
Ti—O(3'')	$2.20 \pm 0.07$ (1)
Ti—O(1')	$2.06 \pm 0.04$ (1)
O(1)—O(1')	$2.41 \pm 0.06$ (1)
O(1)—O(2)	$2.70 \pm 0.06$ (1)
O(2)—O(3'')	$3.15 \pm 0.08$ (1)
O(3'')—O(1')	$2.92 \pm 0.08$ (1)
O(1)—O(3)	$2.87 \pm 0.08$ (2)
O(2)—O(3)	$2.66 \pm 0.08$ (2)
O(3)—O(3'')	$2.69 \pm 0.10$ (2)
O(3)—O(1')	$2.87 \pm 0.08$ (2)
Ti—Ti'	$3.07 \pm 0.02$
Ti—Ti''	$3.15 \pm 0.02$

The Th atoms, binding the sheets together, are located in octahedral interlayer positions. Although the Th-O bonds are not significantly different, two of  $2.36 \pm 0.04 \text{ \AA}$  and four of  $2.35 \pm 0.05 \text{ \AA}$ , the octahedron is far from regular (Table 6). Further away at  $2.96 \pm 0.07 \text{ \AA}$  are the two symmetry related atoms O(3), but they are unbonded according to Pauling's electrostatic bond length criterion. If they were bonded, the coordination

would be eightfold, a hexagonal bipyramid. Thorium usually is in cubic coordination in oxides, and we can find no previous report of an environment similar to the present one.

### Discussion

Most  $\text{AB}_2\text{O}_6$  compounds fall into a small number of distinct groups (Wyckoff, 1965, p. 361 *et seq.*) with little or no obvious resemblance to the present case. Since the lattice constants for low temperature  $\text{UTi}_2\text{O}_6$  recorded by Schröke (1958) were considered to be characteristic of the columbite structure, the diffraction pattern for low temperature  $\text{ThTi}_2\text{O}_6$  (Perez y Jorba *et al.*, 1961) should perhaps be reassessed with this in view. Although  $\text{Th}^{4+}$  and  $\text{U}^{4+}$  are much larger than is usual for the A ions in this particular class, the columbite structure, which is built up from layers of hexagonally close-packed oxygen atoms, might be sufficiently elastic to provide sites of suitable size for these large ions and for the much smaller  $\text{Ti}^{4+}$  ions as well.

Compounds of this type, however, generally contain  $\text{Nb}^{5+}$ ,  $\text{Ta}^{5+}$  or  $\text{Sb}^{5+}$  in the B positions. On the other hand the presence of octahedra joined by edges in pairs, or in linear groups of three, is a much more characteristic feature of titanates (Andersson & Wadsley, 1962) and may ultimately prove to be just as important a structure-determining criterion as the more conventional considerations of ionic size, charge and lattice energy. It was not altogether surprising to find that  $\text{ThTi}_2\text{O}_6$  could be related to the anatase form of  $\text{TiO}_2$ , which is shown in Fig. 4(b). If we imagine this latter structure to be sliced along the (101) direction at intervals of one unit cell, the sheets of octahedra are identical with those in  $\text{ThTi}_2\text{O}_6$  shown in Figs. 3 and 4(a). The relative positions of adjacent sheets give rise to the large flattened octahedral holes into which the Th ions fit, and in so doing provide charge neutrality and maintain structural stability.

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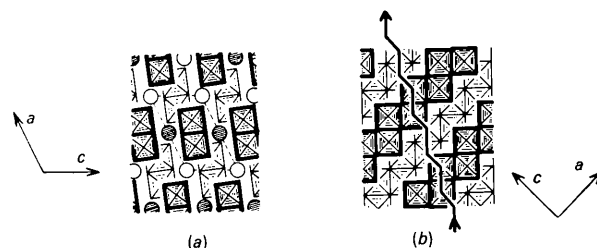


Fig. 4. (a) Idealized octahedral drawing of  $\text{ThTi}_2\text{O}_6$  projected on to (010). The Th atoms are drawn as circles. (b) Idealized drawing of  $\text{TiO}_2$  (anatase). The row of octahedra highlighted with a thick arrowed line is common also to (a). The axial directions are shown by the smaller arrows.

for a period of study leave, and A. J. Gaskin and L. S. Williams for having arranged it. We are grateful to H. O. Bielstein for kindly preparing the specimens.

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